

# The Fault Detection Model of Electric Power Systems Using Systematic Stochastic Petri Nets

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## Abstract:

This paper proposes the modeling of electric transmission power network protection system using Systematic Stochastic Petri Nets (SSPNs). SSPNs, which own the perfect ability of modeling, are used in order to found electric power system faults detection model. Commonly, in substation function, when the electric power system declines, much of switch act data, fault data and alarm data will be carry over from the protection devices to the Supervisory Control and Data Acquisition (SCADA) system, most of them are right while some of them maybe wrong. It is a difficult objective for the operator in order to select the wrong one amidst so much data. Fault detection model is come up with in order to get the right detection result of the fault zone. By the virtue of the substation fault detection, the operator briskly understands the important data and takes correct actions in time. The result of simulation indicates that the scheme has good performance in real time substation fault detection.

Key words: Fault Detection, Protection System, Electric Transmission Power Network, SSPNs

# **1. Introduction**

Fault detection of electric power system is a process of discriminating faulted system components by tripping of protective relays and circuit breakers. Conventionally, fault detection in substation is done by human operator, it is crucial for dispatchers to briskly prediction the fault section in substation before starting restorative actions via the Supervisory Control and Data Acquisition (SCADA) data by their experience. In this circumstance, it is rather difficult to detect fault briskly and exactly merely by human operator with their experience. So as to distribute the fault detection result briskly, obviously and exactly. There are many methods, such as artificial neural networks, genetic algorithms, tabu search, logic reasoning and expert system, [1-2] which have been enforced to fault detection of electric power system. While using these artificial intelligence technologies in order to detect the substation faults, errors are commonly run across in their fault detection process [3-4]. Since these models do not represent the change of the substation configuration, or could not identify the error of the input signal, or needing much of training.

Systematic Stochastic Petri Nets (SSPNs) are a flexible, visualized graphical mathematical modeling tool able to do modeling many systems, particularly discrete event system [5]. They can be enforced to many aspects of electric power system. Much as electric power systems are continuous time systems from a macro power transmission approach, some operating procedures, such as contingencies associated with system change from one state to another state, switch action or relay can be viewed as a set of discrete events. Hence, the systems are made up of those procedures can be considered as discrete event systems, such as switching sequence action and

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protection system, from a micro operating approach. In substation, when a fault happened, associated circuit breakers and switches are tripped, it is a typical discrete dynamic process, and SSPNs have been used in fulfilling fault detection. SSPNs are powerful for real time detection by virtue of its obvious graphical models. Providing a good model is a significant and central task. In this paper, a SSPNs model is suggested based on paper [6] in order to carry out substation fault detection. The suggested fault detection method is carried out using the information of circuit breakers and protective relays. After they have reach their final state, and the fault section can be detected from the fired SSPNs of its final state. The detection process is very fast and simple.

# 2. Modeling Method of SSPNs

## 2.1. SSPNs definition

SSPNs are a one of several mathematical and graphical representations of discrete distributed systems. As a modeling language, it graphically depicts the structure of a distributed system as a directed bipartite graph.

The SSPNs are a directed graph;  $C = (P, T, I, O, M_0)$  where [7];

 $P = \{p_1, p_2, \dots, p_m\}$  is a finite set of places,

 $T = \{t_1, t_2, \dots, t_m\}$  is a finite set of transitions,  $P \cup T \neq \emptyset$ , and  $P \cap T = \emptyset$ ;

 $I = (P X T) \rightarrow N$  is an input function that defines directed arcs from places to transitions, where N is a set of non negation integers;

 $O = (P X T) \rightarrow N$  is an output function that defines directed arcs from transitions to places,  $M_0 = P \rightarrow N$  is the initial marking.

## 2.2. Graphical model of SSPNs

The graphical model of SSPNs consists of nodes and arcs that represent different physical concepts. The node set is composed of two independent subsets, place set  $P = \{p_1, p_2, ..., p_n\}$ , and transition set  $T = \{t_1, t_2, ..., tn\}$ . Each node corresponds to only one place element  $p_i$  or transition element  $t_i$ . Two different kinds of weighted directional arcs are included in arc set, which are named as the subset of input arcs and the one of output arcs. The token number of each place is marked by a figure of dots in each place circle, which may not only represent a certain material resource but also denote some corresponding information resource [8].

The arc weight is marked with a figure and its default value is one. Figure 1 shows a simple SSPNs structure where  $p_1$  and  $p_2$  represent places and  $t_1$  represents transition, and the dot in place  $p_1$  represents the initial marking (token). The structures of SSPNs are static, and its dynamic properties are defined by transitions firing as well as transition of the tokens. The firing will move the tokens from the transitions input places to its output places [9].



Figure 1. Simple SSPNs structure

#### 2.3. Matrix representation of SSPNs

Defining two matrices  $D^-$  and  $D^+$  representing input and output functions is alternative to defining a SSPNs as (P, T, I, O, M<sub>0</sub>). Each matrix has *m* rows (two per transition) and *n* columns (one per place).  $D^-$  defines transition inputs,  $D^+$  defines transition outputs. The matrix form to define SSPNs; (P, T,  $D^-$ ,  $D^+$ , M<sub>0</sub>) allows giving definitions in terms of vectors and matrices [7]. Let us define a single vector e[j] of dimension *m* containing zeros in all places but the one corresponding to the transition being started at the moment. Apparently, the transition is permitted if  $\mu \ge e[j] \cdot D^-$ , the result of the startup of the j-th transition can be described as follows  $\mu' = \mu + e[j] \cdot D$ , and where  $D = (D^+ - D^-)$  is the incidence matrix.

#### 2.4. A simple fault detection of SSPNs model for substation

Figure 2 indicates a purified substation network. There are two outgoing feeders,  $N_1$  and  $N_2$ , just observe feeder  $N_1$ , when a fault happened at node  $N_1$ , the main protection  $R_1$  and circuit breaker CB<sub>1</sub> employs in order to clear the fault. If CB<sub>1</sub> failed to employ, the first backup protection  $R_2$ ,  $R_3$  and circuit breaker CB<sub>2</sub>, CB<sub>3</sub> will employ in order to clear the fault. If CB<sub>2</sub> or CB<sub>3</sub> fails to clear the fault, the second backup protection and its corresponding circuit breakers will employ.



Figure 2. Purified substation network

So far as the aloft rules of protection configurations, the SSPNs model of the net for fault detection is indicated in figure 3. In this model, observe node N<sub>1</sub>, place R<sub>1</sub>, CB<sub>1</sub> present the main protection and its circuit breakers action state. Place R<sub>2</sub>, R<sub>3</sub>, CB<sub>2</sub>, CB<sub>3</sub> present the primary backup protection and its circuit breakers action state. By the same, place R<sub>4</sub>, R<sub>5</sub>, R<sub>6</sub>, R<sub>7</sub>, CB<sub>4</sub>, CB<sub>5</sub>, CB<sub>6</sub>, and CB<sub>7</sub> present the secondary backup protection and its circuit breakers action state. By the same, place R<sub>4</sub>, R<sub>5</sub>, R<sub>6</sub>, R<sub>7</sub>, CB<sub>4</sub>, CB<sub>5</sub>, CB<sub>6</sub>, and CB<sub>7</sub> present the secondary backup protection and its circuit breakers action state. Place B<sub>1</sub>, B<sub>2</sub>, C<sub>1</sub>, C<sub>2</sub>, C<sub>3</sub> and C<sub>4</sub> are virtual nodes and have no physical meaning. In this model, the incipient token distribution is verified with respect to the information received from the control center and SCADA system. If the information illustrates that the relay R<sub>n</sub> (R<sub>1</sub>, R<sub>2</sub>, R<sub>3</sub>, R<sub>4</sub>, R<sub>5</sub>, R<sub>6</sub> and R<sub>7</sub>) and circuit breakers CB<sub>n</sub> (CB<sub>1</sub>, CB<sub>2</sub>, CB<sub>3</sub>, CB<sub>4</sub>, CB<sub>5</sub>, CB<sub>6</sub> and CB<sub>7</sub>) has employed, then there will be an incipient token set in corresponding place.



Figure 3. SSPNs model for purified substation network

After finishing incipient token distribution, the transition matching the circumstance will be fired. The firing circumstance of each transition is defined as follows [2];

If there is a token in both place  $CB_n$  and place  $R_n$ , transition  $tr_n$  (n = 2, 3, 4, 5, 6, 7) will be fired. If there is a token in each of place  $R_1$  and  $CB_1$ ,  $B_1$  and  $B_2$ ,  $C_1$  and  $C_2$ ,  $C_3$  and  $C_4$  respectively, transition  $T_1$ ,  $T_2$ ,  $T_{3a}$  and  $T_{3b}$  will be fired. The token will redeliver in the net after a series firing of transition until no transition can be fired, and then the net arrives the stable status. The fault section can be forthrightly derived from the net at that time. The measure rule is as follows; if there are tokens in place N, then node N is fault section.

## 3. Fault Detection Methodology

## 3.1. Detection procedure

At modeling in SSPNs, places denote certain system states, while transitions denote actions taking place in the system. The system may generate certain actions being in a certain state; and, vice versa, execution of a certain action shifts the system from one state to another. The current system state is defined by the SSPNs marking, the location of marks in the net places. Execution of actions in the system is defined as transition actuations in SSPNs. Actuation of transitions generates new marking, thus, generating new location of marks in the net.

The SSPNs shown in Figure 3 has a complex structure due to the existing parallel processes. In such cases, decomposition of the SSPNs are expedient, since the parallelism conditions increase in the number of system states in geometric progression accompanied by the increase of positions of each branch. Decomposition ensures decrease the number and complexity of synthesized logical sequences and more efficient realization of the sequences in distributed systems. When using decomposition, each branch is treated as a separate subnet. Decomposition results in a set of subnets and a net coordinating the starting of the subnets. The SSPNs decomposition in the automated control system of fault detects will result in functional subnets of the initial SSPNs as shown in Figure 4.



Figure 4. Functional subnets of initial SSPNs model

Let us perform the matrix analysis the subnets  $Z_1 \rightarrow Z_{10}$ . The subnet  $Z_1$ , as shown in figure 4, has 4 states (R<sub>7</sub>, CB<sub>7</sub>, C<sub>4</sub>, B<sub>2</sub>) and 2 transition (t<sub>7</sub>, T<sub>3b</sub>). Let us plot the matrix of inputs, the matrix of outputs and the incidence matrix for the subnets  $Z_1 \rightarrow Z_{10}$ .

$$\begin{split} Z_{1} &= D_{-1}^{-} - D_{-1}^{+} \rightarrow D_{-1}^{-} = \begin{bmatrix} 0 & 0 & 1 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}; \quad D_{-1}^{+} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 1 \end{bmatrix}; \rightarrow Z_{1} = \begin{bmatrix} 1 & 1 & -1 & -1 \\ 1 & 1 & -1 & 1 \end{bmatrix}; \\ Z_{2} &= Z_{1} \rightarrow Z_{2} = \begin{bmatrix} 1 & 1 & -1 & -1 \\ 1 & 1 & -1 & 1 \end{bmatrix}; \quad D_{-1}^{+} = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}; \rightarrow Z_{3} = \begin{bmatrix} 1 & -1 & -1 \\ 1 & 1 & -1 & 1 \end{bmatrix}; \\ Z_{3} &= D_{-3}^{-} - D_{+3}^{+} \rightarrow D_{-3}^{-} = \begin{bmatrix} 0 & 1 & 1 \end{bmatrix}; \quad D_{-1}^{+} = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}; \rightarrow Z_{3} = \begin{bmatrix} 1 & -1 & -1 \end{bmatrix}; \\ Z_{4} &= D_{-4}^{-} - D_{+4}^{+} \rightarrow D_{-4}^{-} = \begin{bmatrix} 0 & 0 & 0 \end{bmatrix}; \quad D_{-4}^{+} = \begin{bmatrix} 1 & 1 & 1 \end{bmatrix}; \rightarrow Z_{4} = \begin{bmatrix} 1 & 1 & 1 \end{bmatrix}; \\ Z_{5} &= D_{-5}^{-} - D_{-5}^{+} \rightarrow D_{-5}^{-} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}; \quad D_{-5}^{+} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}; \rightarrow Z_{5} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}; \\ Z_{6} &= Z_{5} \rightarrow Z_{6} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}; \quad Z_{7} = Z_{8} = Z_{3} \rightarrow Z_{7} = \begin{bmatrix} 1 & -1 & -1 \end{bmatrix}; \quad Z_{8} = \begin{bmatrix} 1 & -1 & -1 \end{bmatrix}; \\ Z_{9} &= Z_{10} = Z_{4} \rightarrow Z_{9} = \begin{bmatrix} 1 & 1 & 1 \end{bmatrix}; \quad Z_{10} = \begin{bmatrix} 1 & 1 & 1 \end{bmatrix}; \end{split}$$

The matrix analysis method ensures vivid demonstration of the application of mathematical apparatus in describing internal logical operations of the fault detection model of electric power systems.

#### 3.2. Detection result analysis

After three times firing of the transition, the net arrives its final stable status. In the final SSPNs model, there is a token in place  $R_1$ ,  $R_2$ ,  $N_1$  respectively. So far as the measure rules of the fault detection, a token in place  $N_1$  means the node  $N_1$  exist fault. Therefore a conclusion can be drawn

that node  $N_1$  is the fault area. The fault is purged by the primary backup protection  $R_3$ , circuit breaker CB<sub>3</sub> and the secondary backup protection  $R_4$ ,  $R_5$ , circuit breaker CB<sub>4</sub>, CB<sub>5</sub>. As a token in place  $R_1$  and  $R_2$  shows that  $R_1$  and  $R_2$  have employed, but their corresponding circuit breakers CB<sub>1</sub>, CB<sub>2</sub> have not employed. Therefore the transition  $T_1$  and  $t_2$  has not fired and the token in  $R_1$ and  $R_2$  has not moved and yet in their place. CB<sub>1</sub> is rejected to act, and the secondary protection must be started. No token in secondary protection  $R_3$  and CB<sub>3</sub> indicates that CB<sub>3</sub> has employed to clear the fault. While  $R_3$ , CB<sub>3</sub> employed,  $R_2$ , CB<sub>2</sub> also should employ as the same level protection. But CB<sub>2</sub> failed in order to employ, so it's corresponding lower level protection and circuit breaker CB<sub>4</sub>, CB<sub>5</sub> employed in place of CB<sub>2</sub> in order to clear the fault.

# Conclusions

The operators of power station control room need to a system to aid and support them to make reasonable decisions during critical situations and reducing the delay of restoration after emergency, a purified SSPNs fault detection system is proposed to deal with a lot of alarms and tripping signals which are sent to the power station control room. The paper proposes a fault detection system based on SSPNs for an electric power system, which includes; load units, power transformers, block bus and station buses. The proposed method can be applied on electric power station through building SSPNs model for each section. Moreover, it can deal with disoperation of the circuit breakers. The proposed method is tested on electric power system to demonstrate its performance and effective. The testing results demonstrate that proposed methods to actual electric power systems. The detection results can be easily drawn from the final stable SSPNs model rather than further reasoning. So, SSPNs model is excellent for substation fault detection.

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